

# Peak Water Demand Study: *Development of Metrics and Method for Estimating Design Flows in Buildings*

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ACEEE 2016 HOT WATER FORUM: PORTLAND, OR  
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# Outline

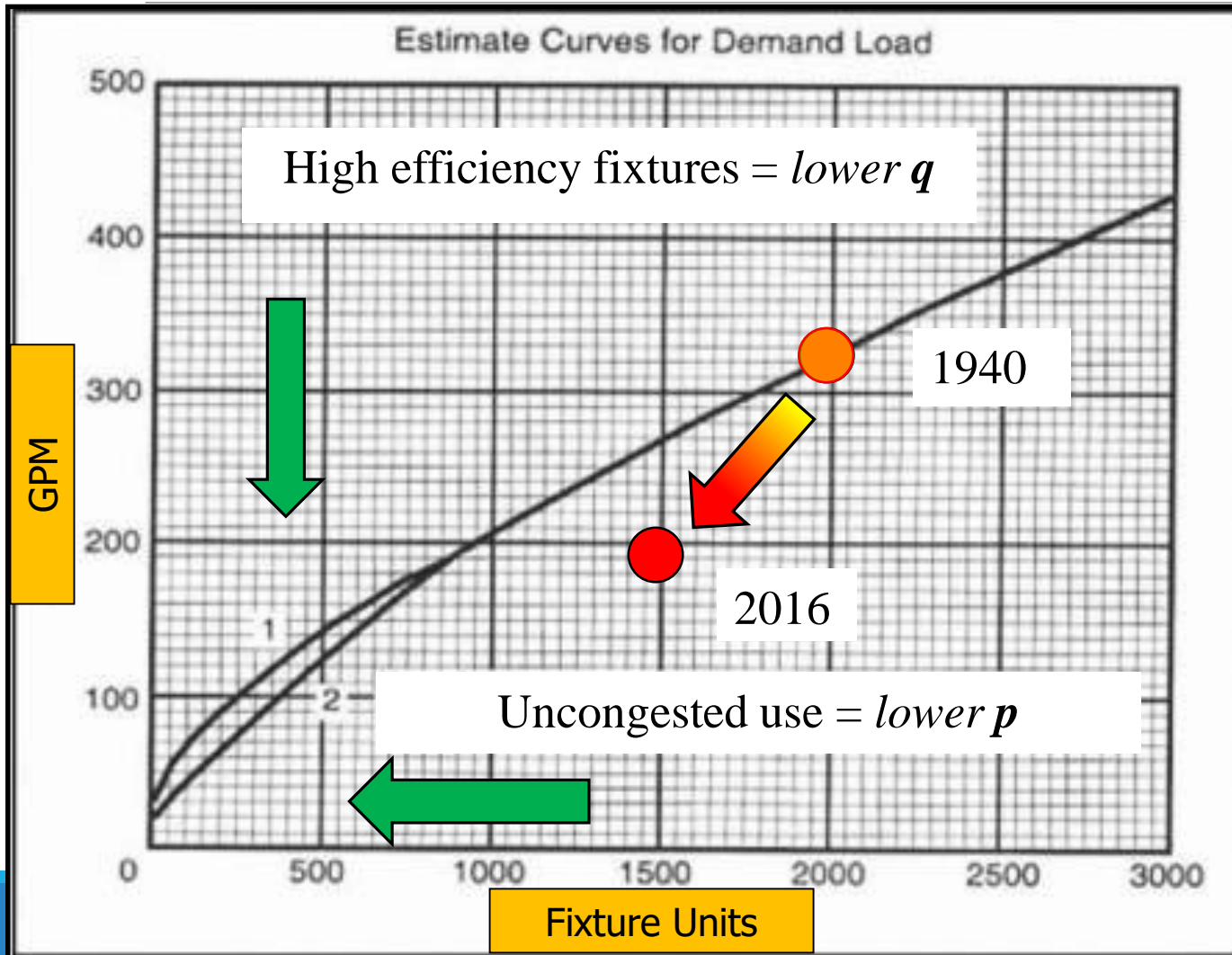
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- ❖ Background
- ❖ Task Group
- ❖ Water Use Database
- ❖ Key Parameters and Considerations
- ❖ Application
- ❖ Conclusion

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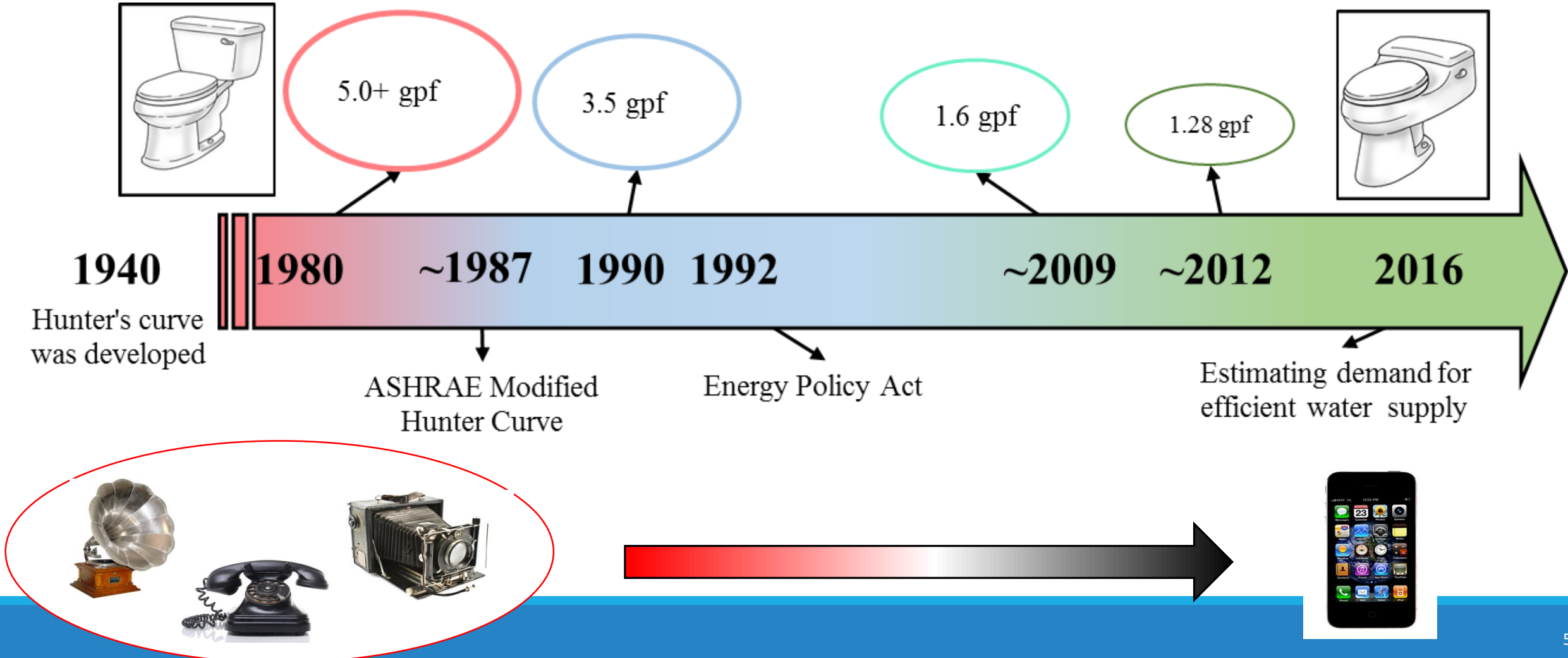
# BACKGROUND

# Hunter's Curve

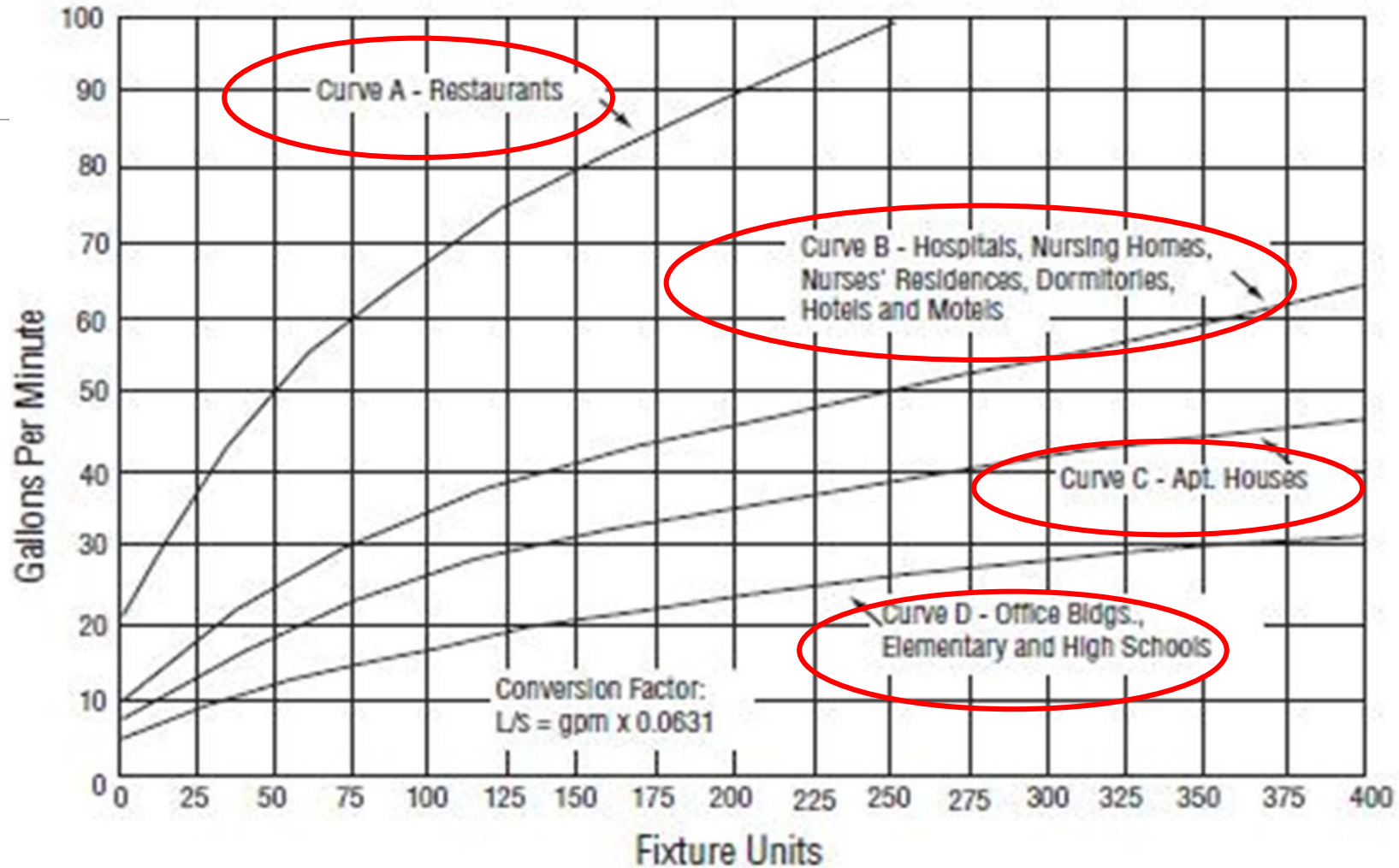


Today, **Hunter's curve** is often faulted for giving overly conservative design....Why?

# Changing Times



# Modified Hunter's Curve(s)



Different curve for different end users



***International Association of  
Plumbing and Mechanical Officials***

**TASK GROUP**



*International Association of  
Plumbing and Mechanical Officials*

# IAPMO Task Group Orders

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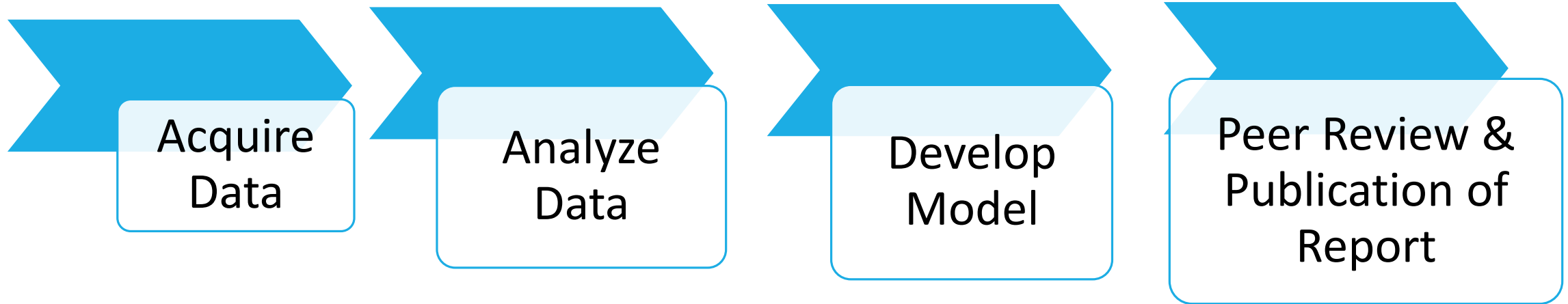
“....will work singularly to develop the probability model to predict peak demands based on the number of plumbing fixtures of different kinds installed in one system.”

**(Bring Hunter into 21<sup>st</sup> Century)**



# Project Activities

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# WATER USE DATABASE

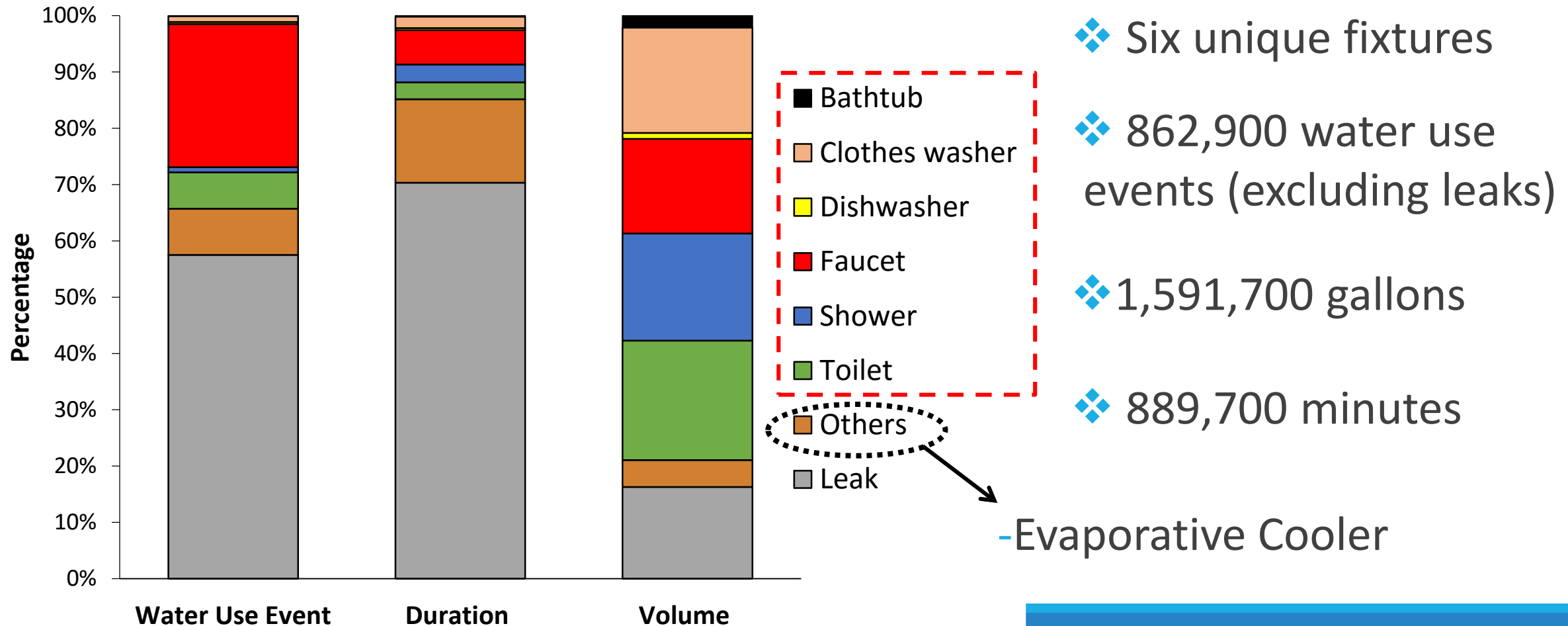


# Database: Location of Homes



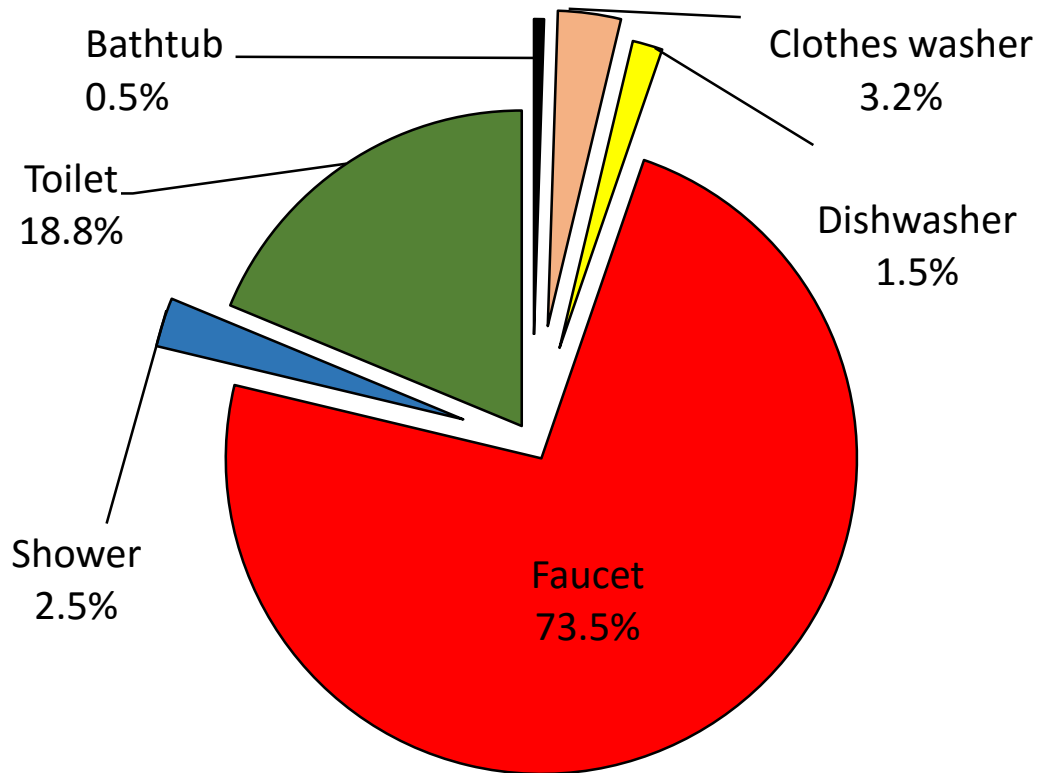
- ❖ Over 1000 households
- ❖ Surveyed between 1996 -2011
- ❖ 2,800 residents
- ❖ 11,350 monitoring days

# Database: Summary of Measured Data

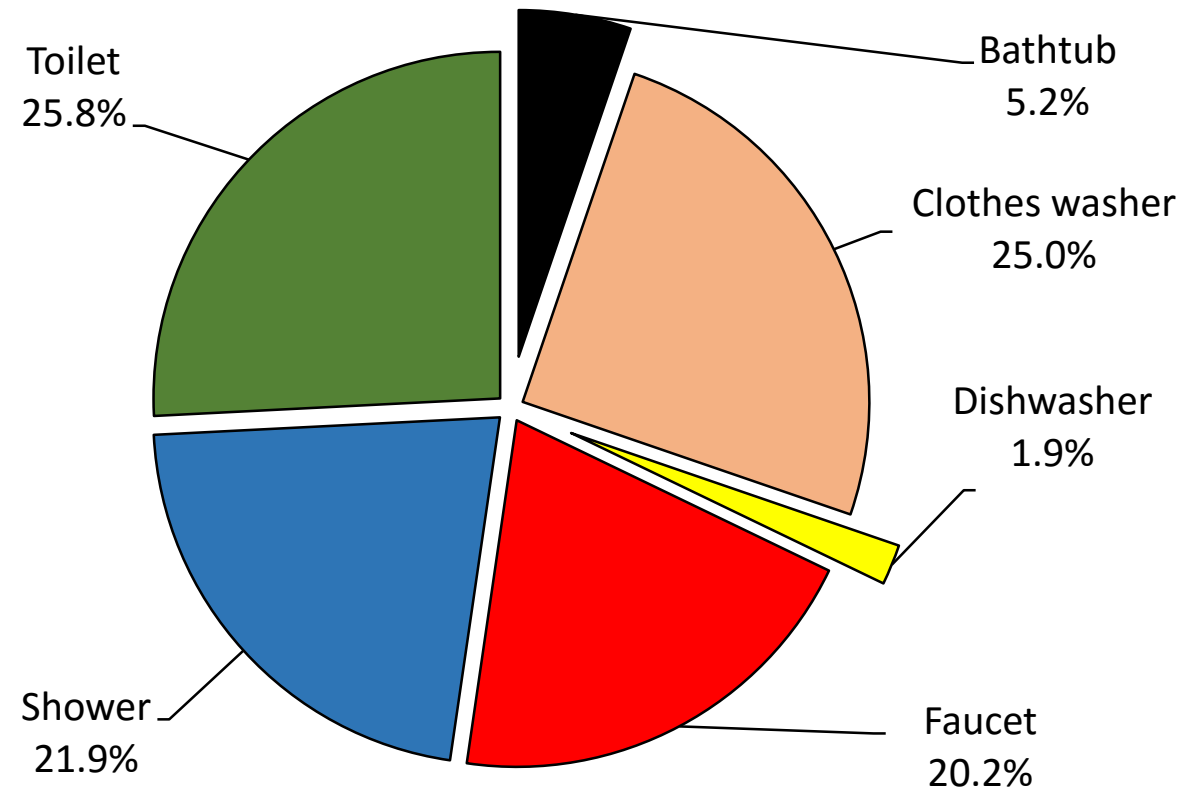


# Database: Details of Water Use at Fixture

FREQUENCY OF FIXTURE USE PER CAPITA PER DAY



VOLUME OF WATER USE PER CAPITA



# Database: Residential Fixture Classification

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Fixture*	Ultra-Efficient	Efficient	Inefficient
Clothes washer (gallons /load)	< 20	20 – 30	> 30
Dishwasher (gallons/cycle)	< 1.8	1.8 – 3.0	> 3.0
Shower (gallon/minute)	< 2.2	2.2 – 2.5	> 2.5
Toilet (gallon/flush)	< 1.8	1.8 – 2.2	> 2.2

\*Bathtubs and faucets were excluded

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# KEY PARAMETERS & CONSIDERATIONS

# Key Fixture Characteristics

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1 -  $n$ : Fixture Count



1

2

3

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$x$

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$n$

2 -  $q$ : Fixture flow rate



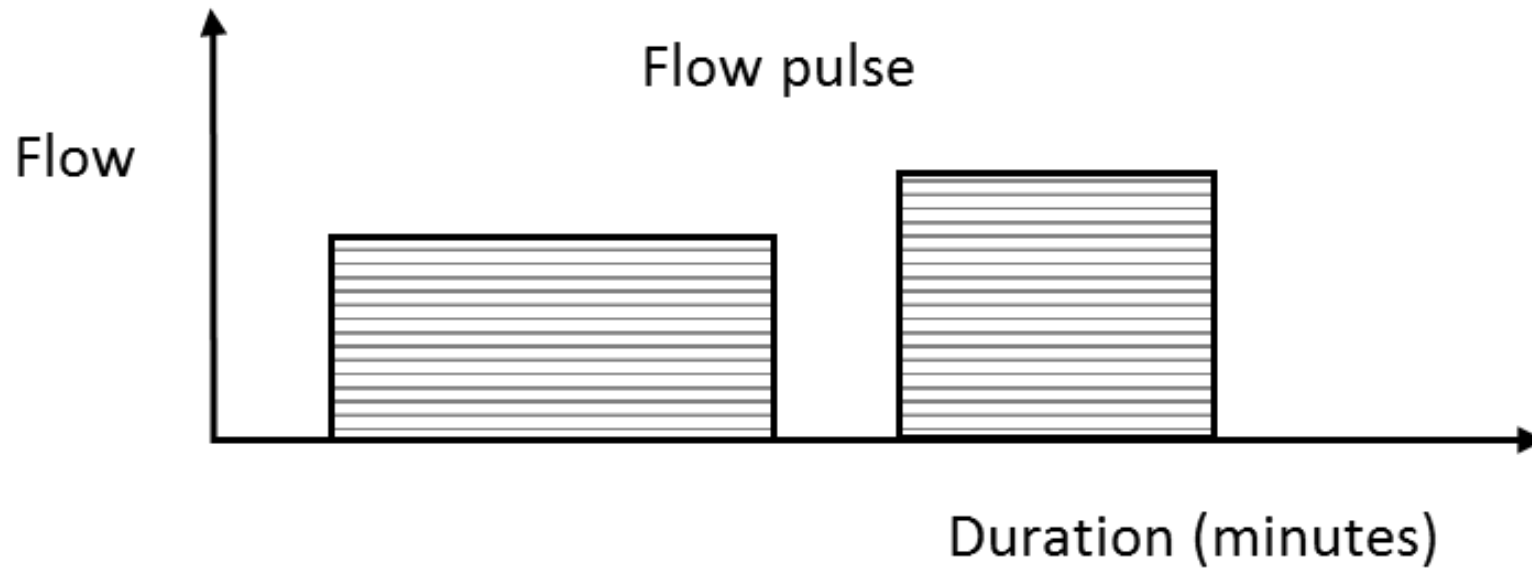
3 -  $p$ : Fixture Probability of use

$$p = \frac{\sum t_i}{T}$$



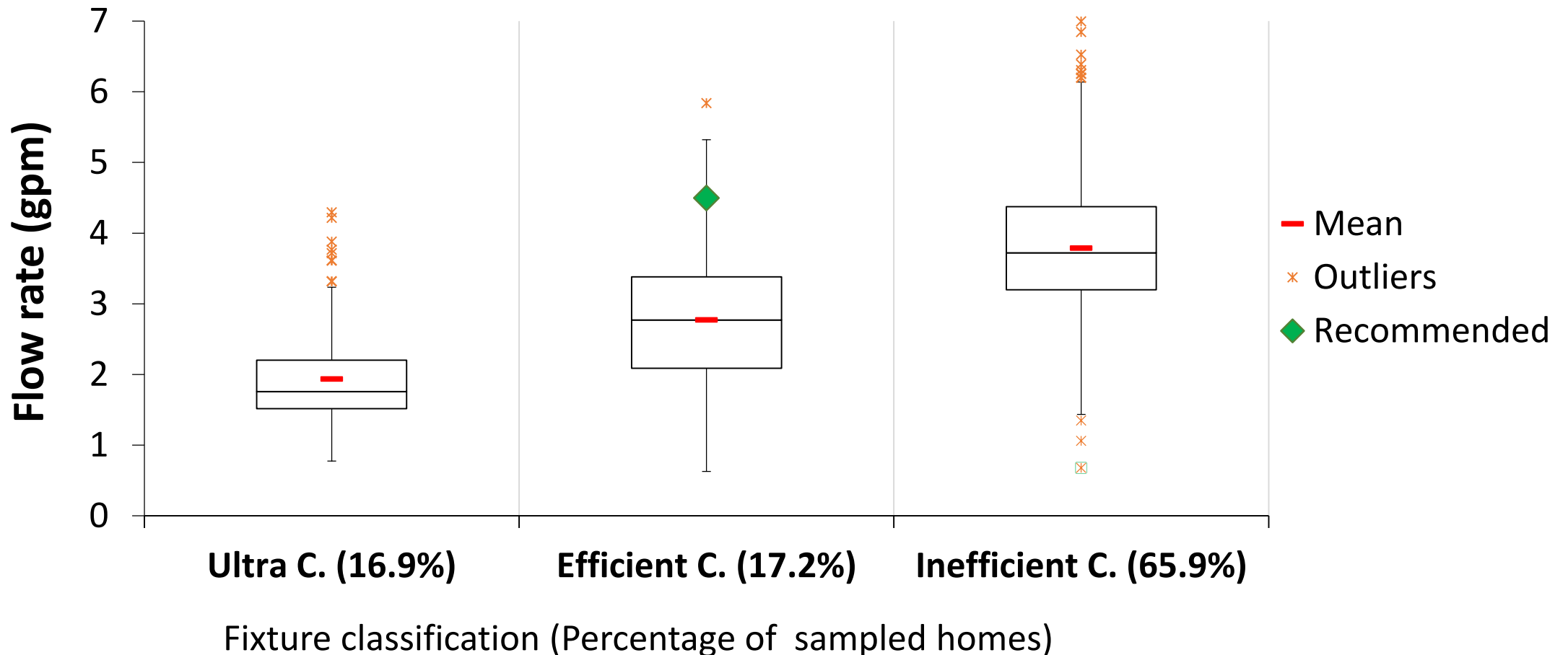
# Computed Fixture Flow Rate; $q$

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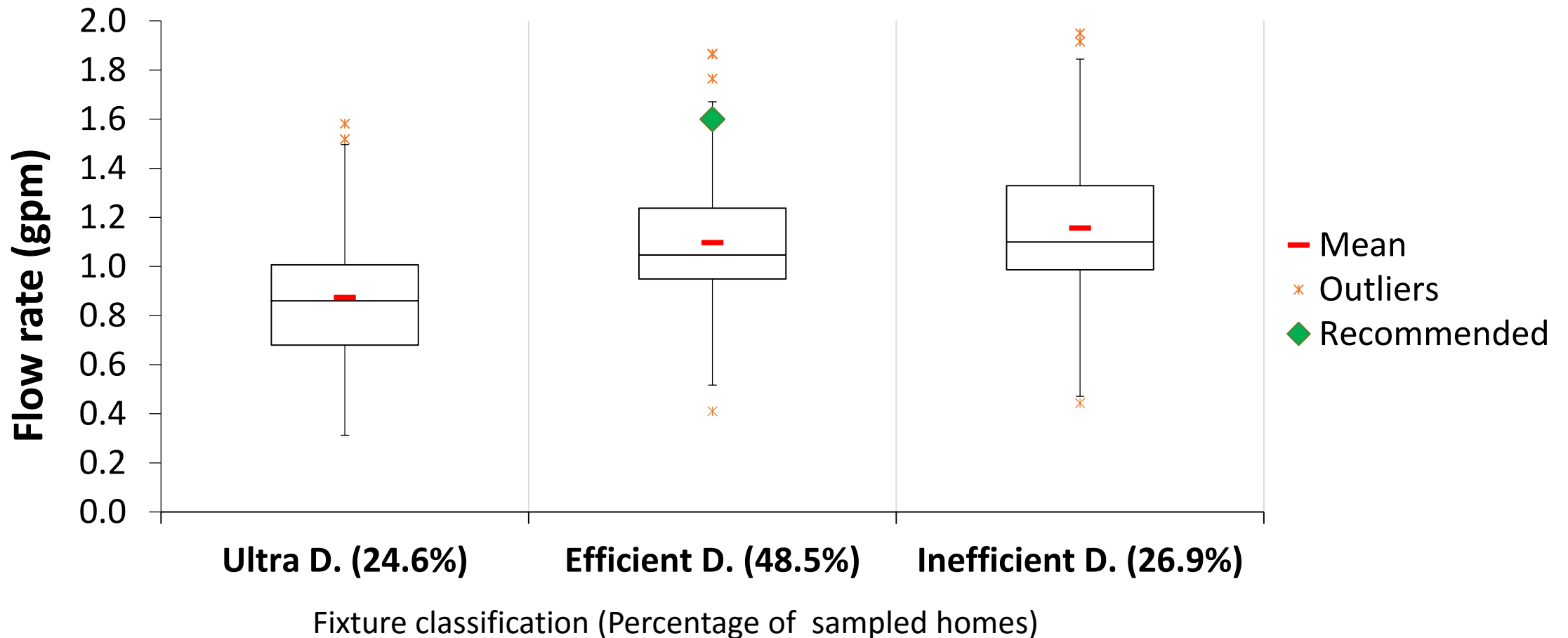


$$q = \frac{\sum \text{Volume of each pulse (gallons)}}{\sum \text{Duration of each pulse (minutes)}}$$

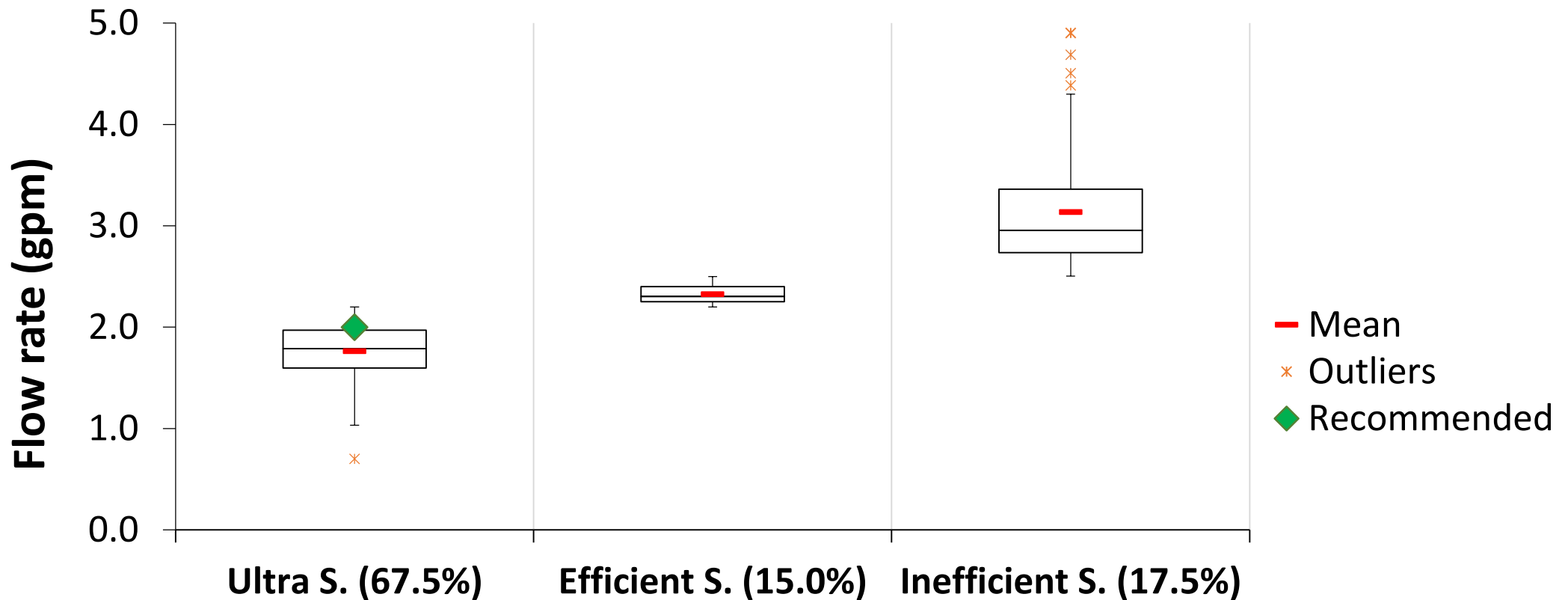
# Clothes Washer Flow Rate



# Dishwasher Flow Rate



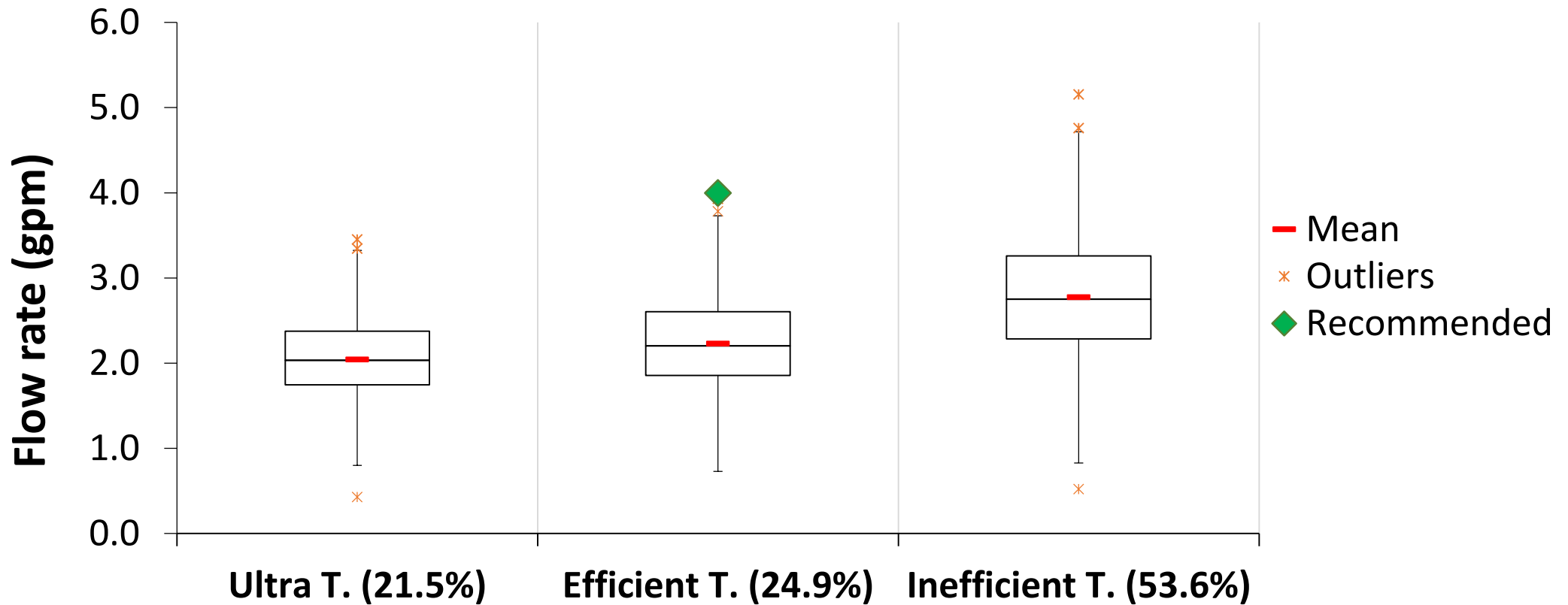
# Shower Flow Rate



Fixture classification (Percentage of sampled homes)

Shower efficiency measured in gallons/minute

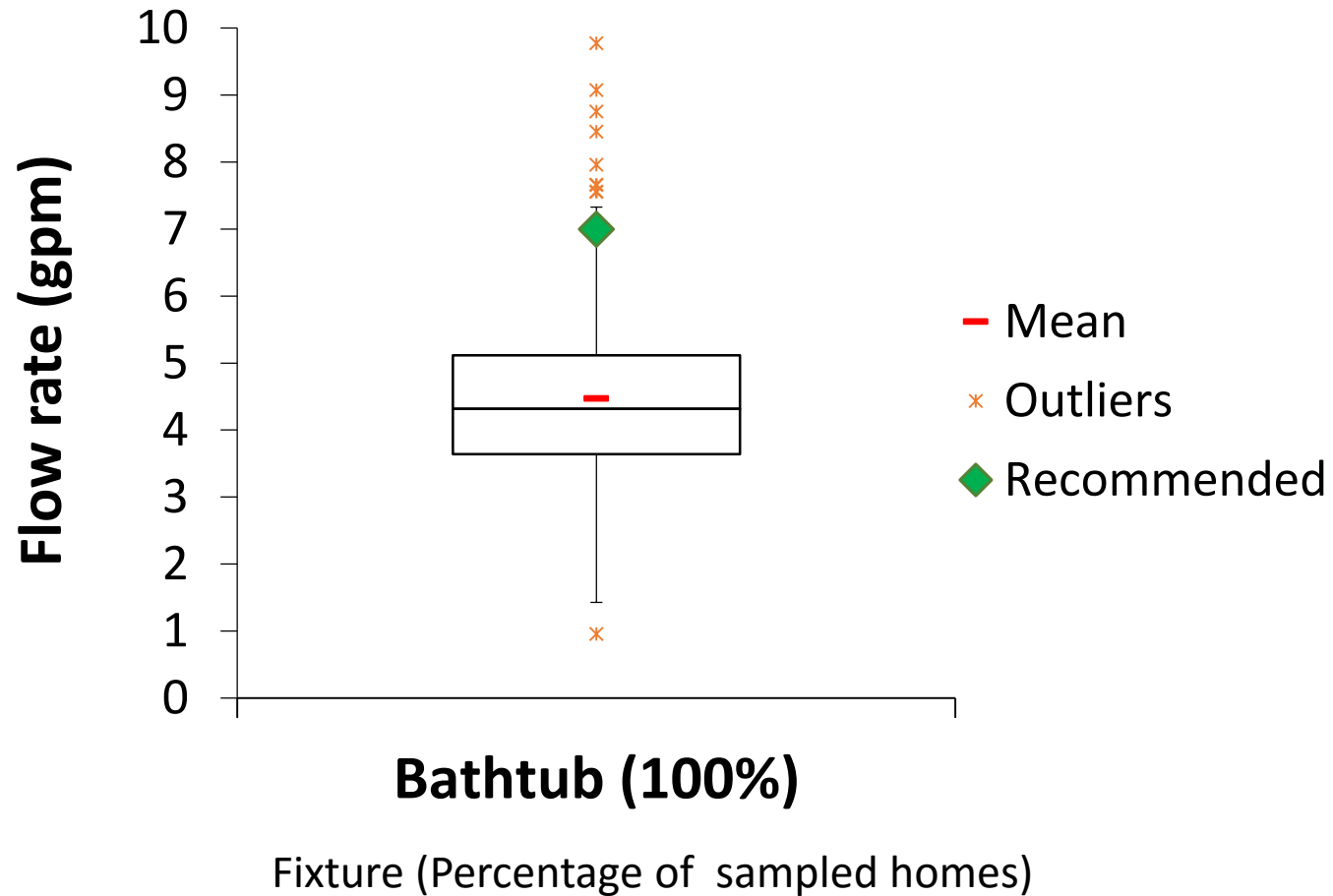
# Toilet (Water Closet) Flow Rate



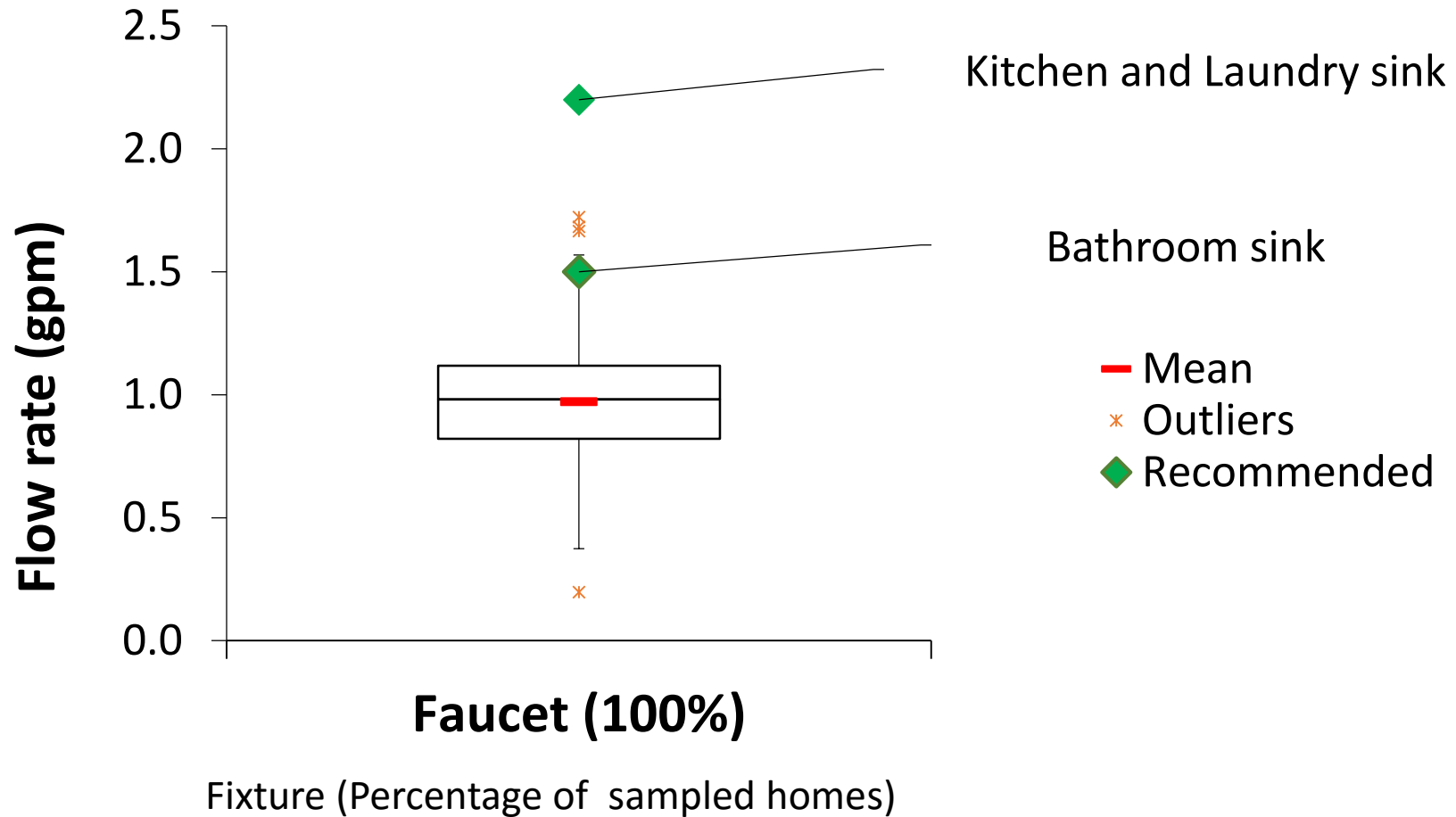
Fixture classification (Percentage of sampled homes)

Toilet efficiency measured in gallons/flush

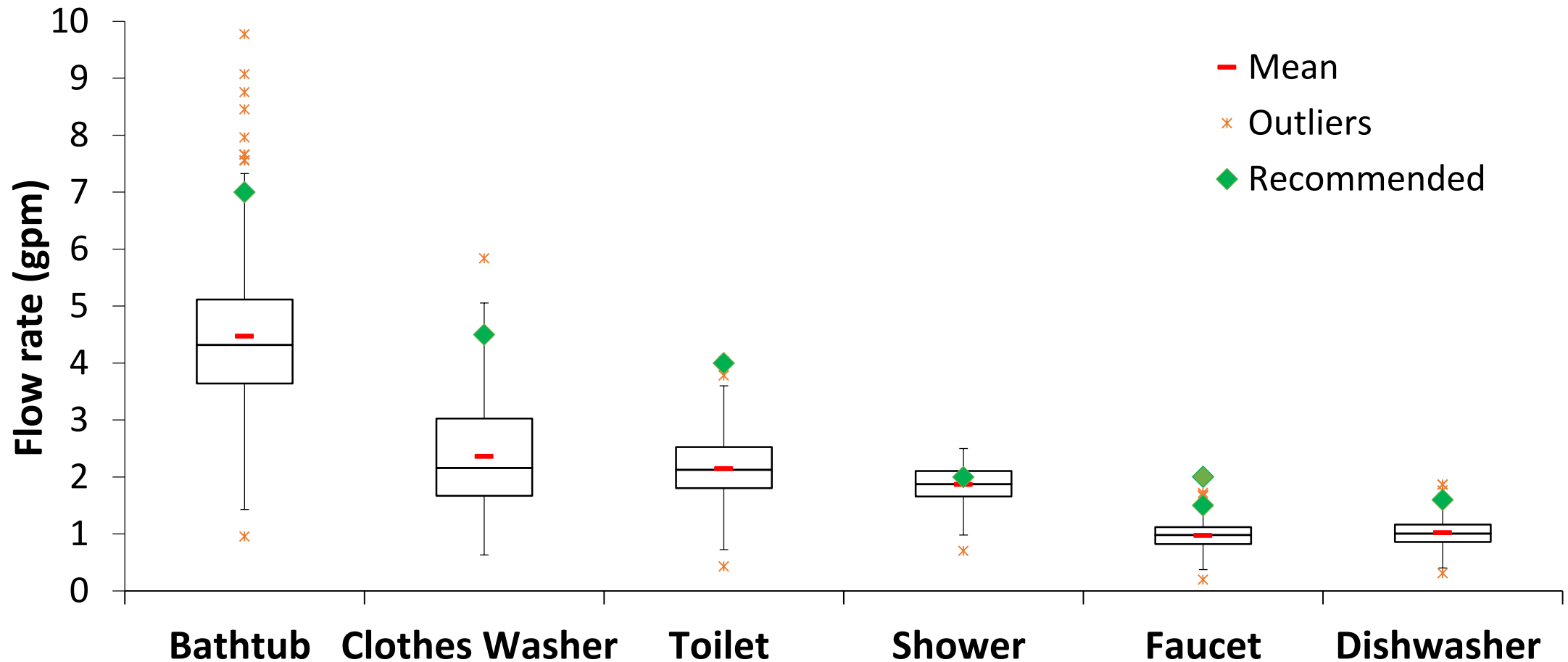
# Bathtub Flow Rate



# Faucet Flow Rate



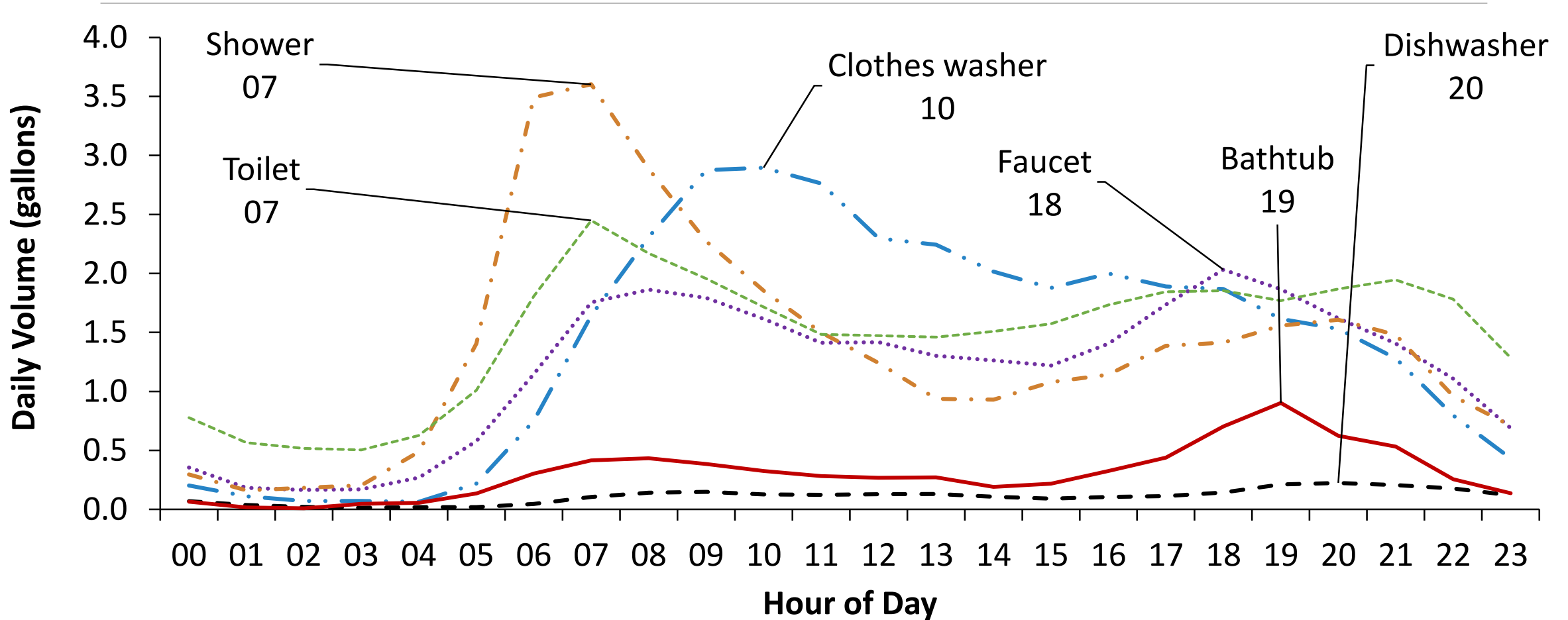
# Summary of “Efficient” Fixture Flow Rate



“Efficient” = Ultra-efficient and Efficient Fixtures

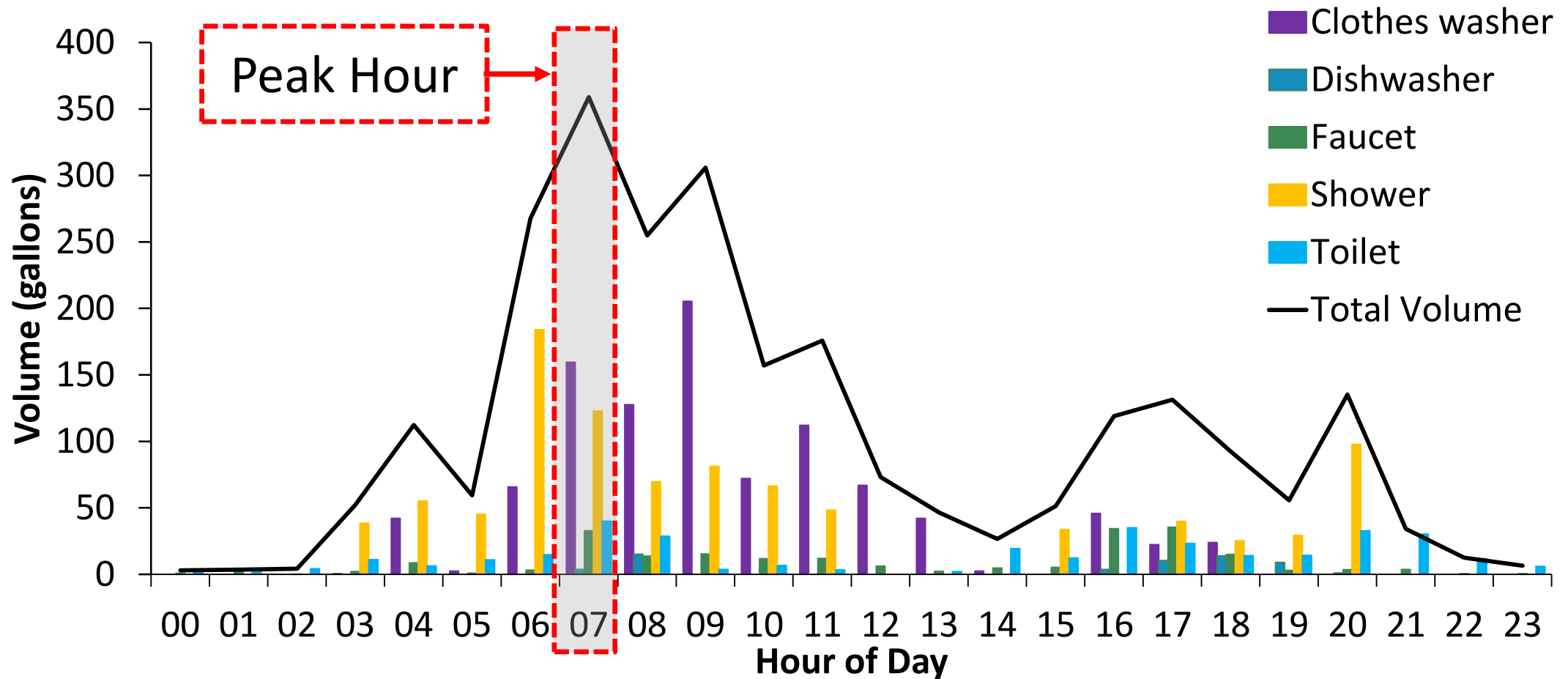


# Peak Hour of Fixture Use (by Volume)

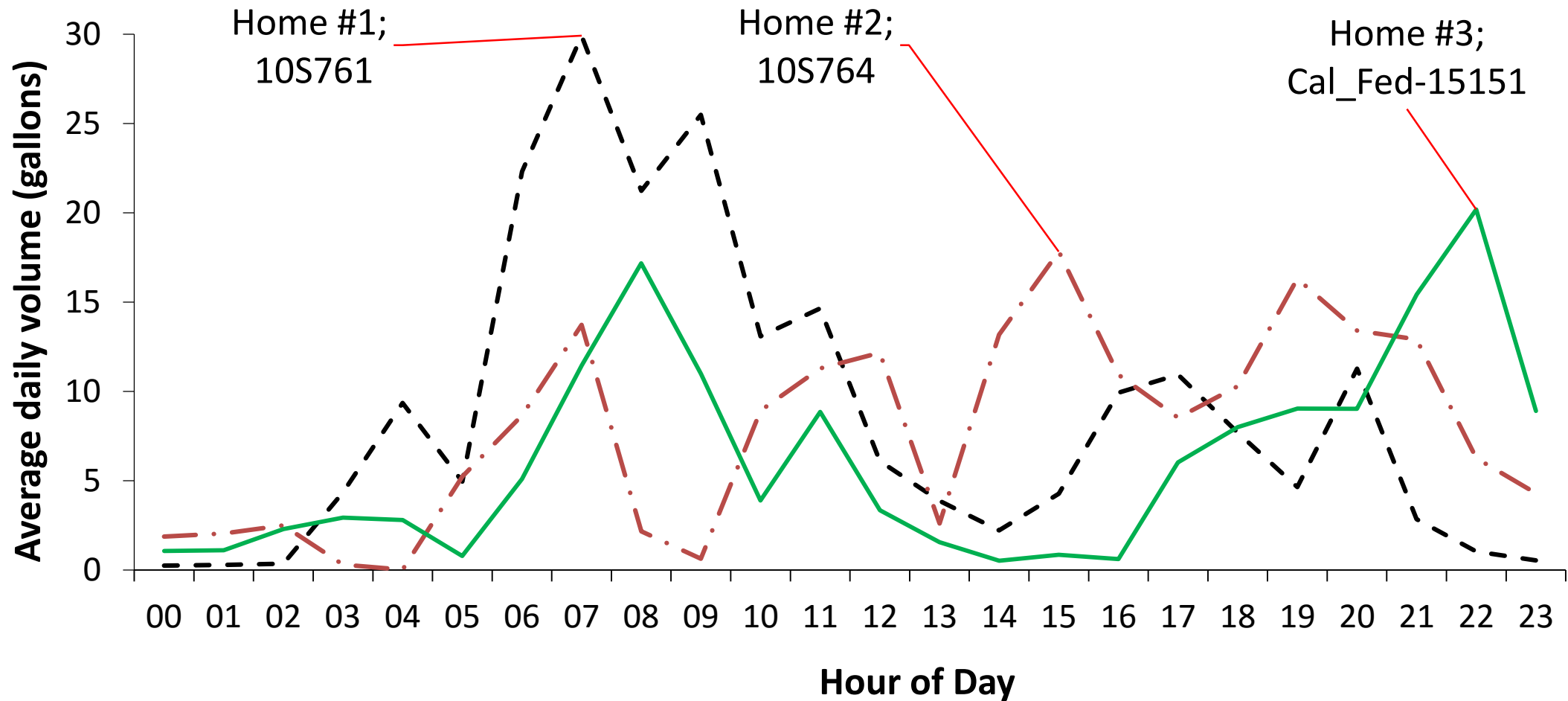


Average hourly volume of water use at a fixture per home per day

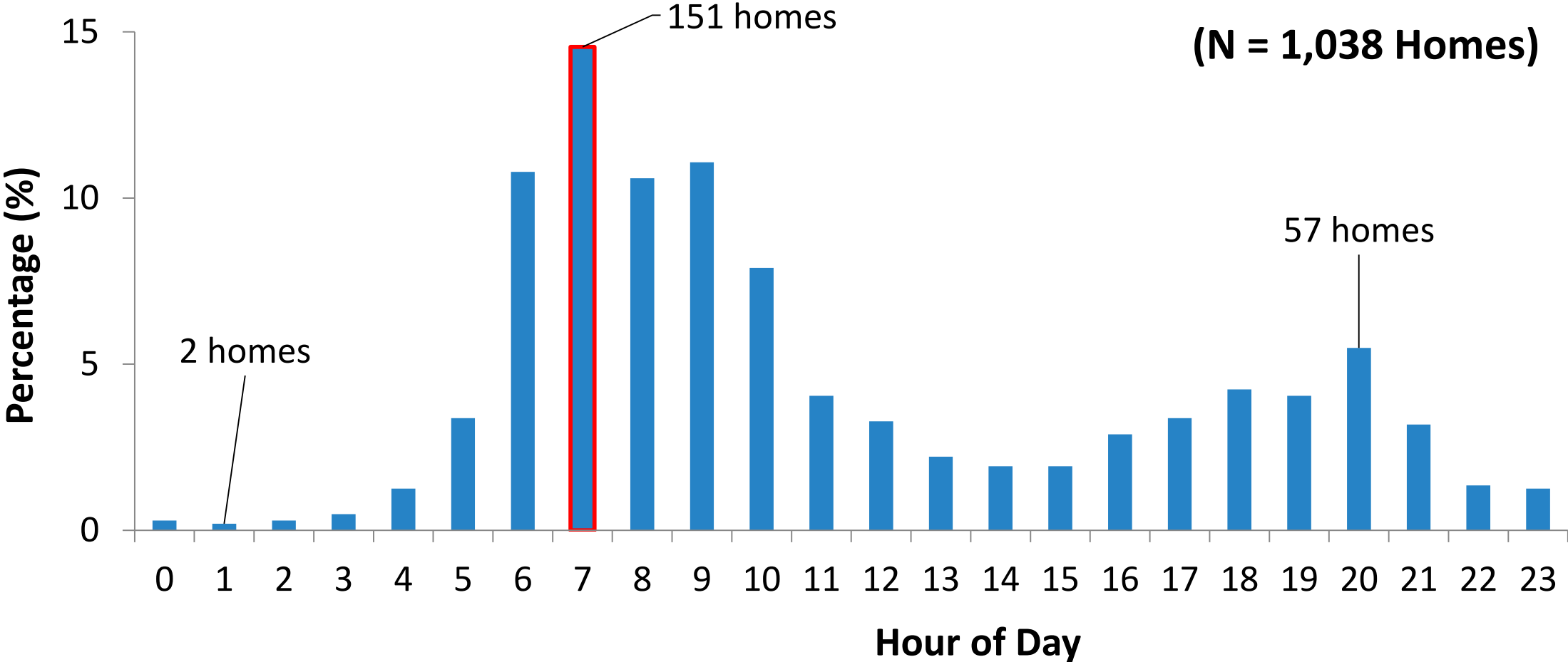
# Single Home 12 Day Water Use Profile (10S761)



# Multiple Homes Water Use Profile (by Volume)



# Distribution of Peak Hour of Water Use



# Peak Hour Probability of Fixture Use

❖ Focused on only efficient fixtures

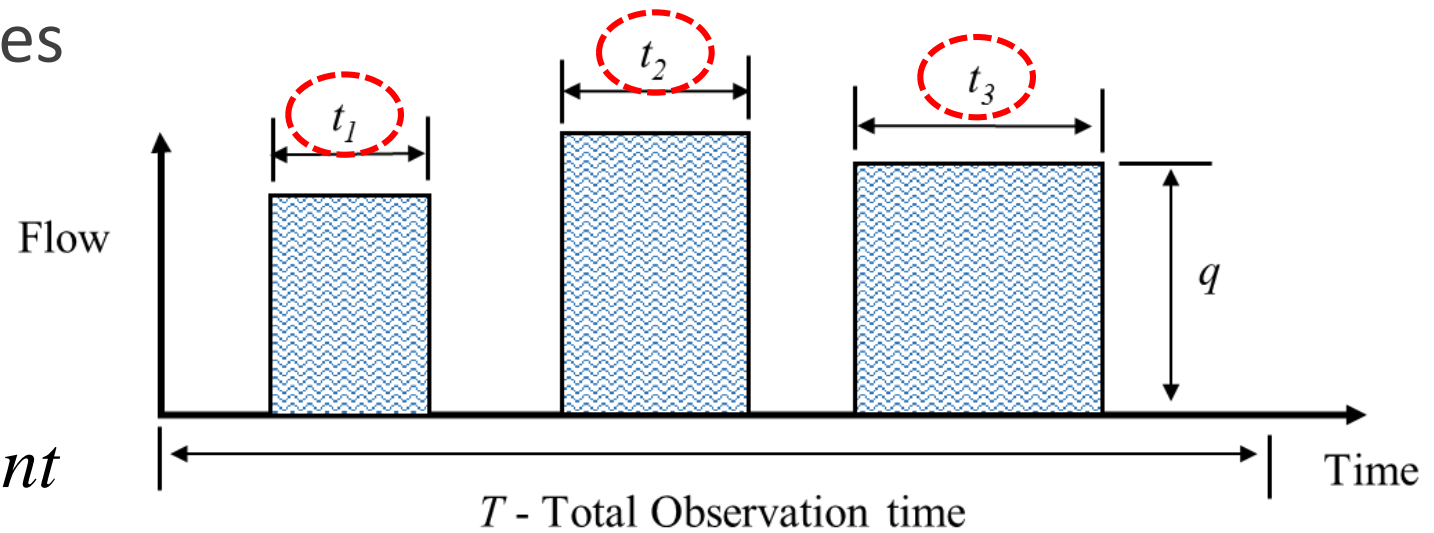
$$p = \frac{\sum_i t_i}{n \cdot D \cdot T}$$

$t_i$  – Duration of  $i^{\text{th}}$  water use event

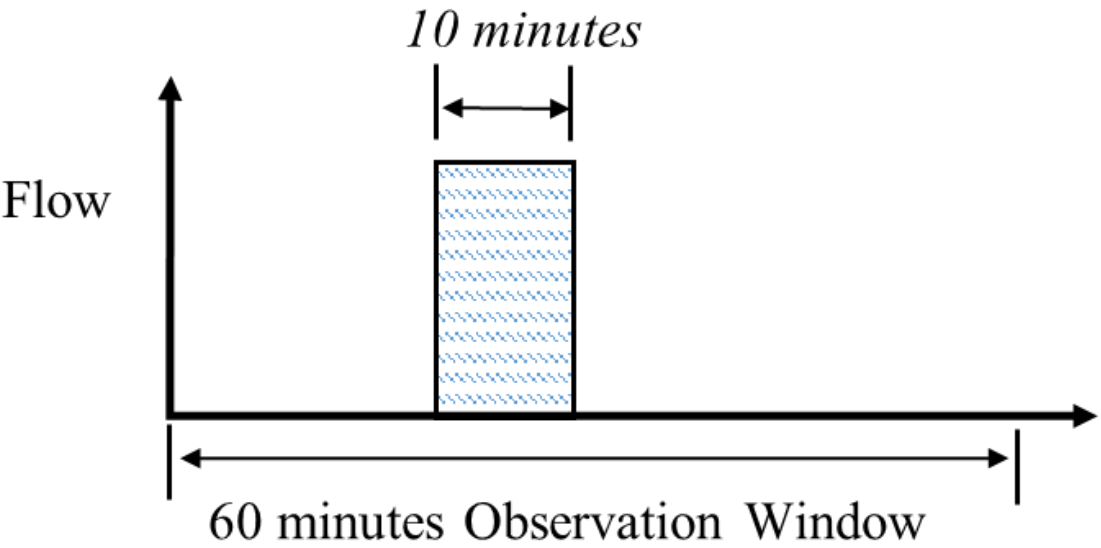
$n$  – Number of fixtures

$D$  – Number of observation days

$T$  – 60 minutes (1 hour observation window)



# Probability of Fixture Use at Individual Homes

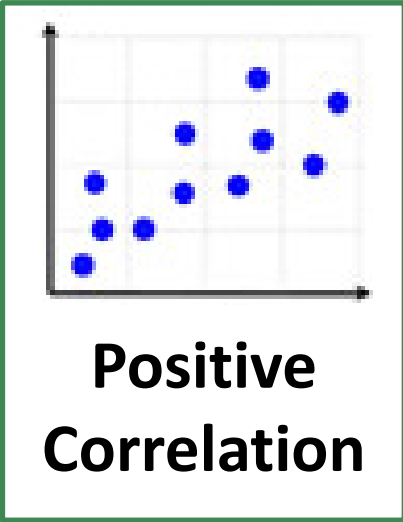


$$p = \frac{\sum_i t_i}{n \cdot D \cdot T}$$

$$p = \frac{10 \text{ minutes}}{1 \text{ fixture} \cdot 1 \text{ day} \cdot 60 \text{ minutes}} = 0.17$$

Considered only efficient fixtures

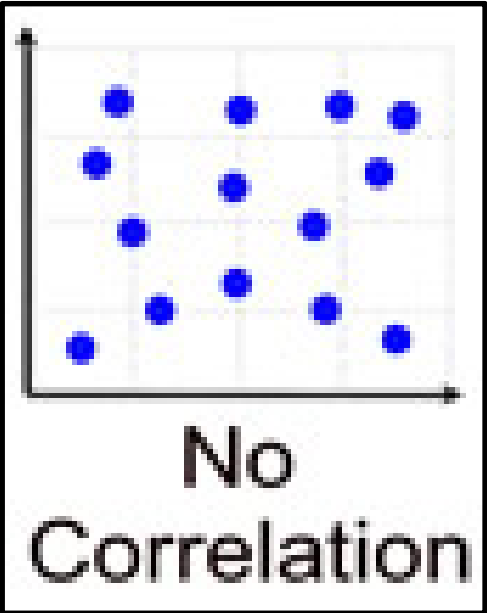
# Probability of Fixture Use – Group of Homes



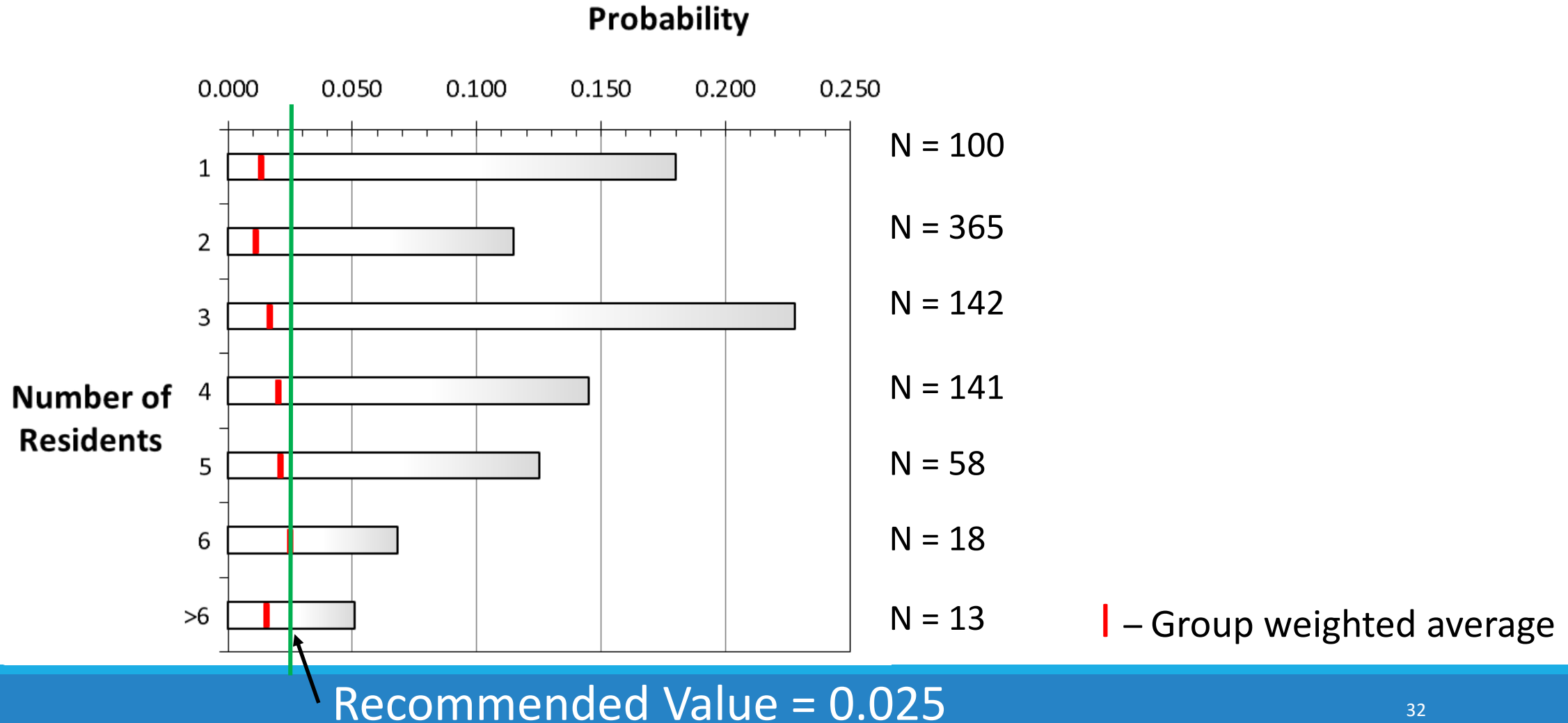
❖ Number of residents

❖ Number of bathrooms

❖ Number of bedrooms

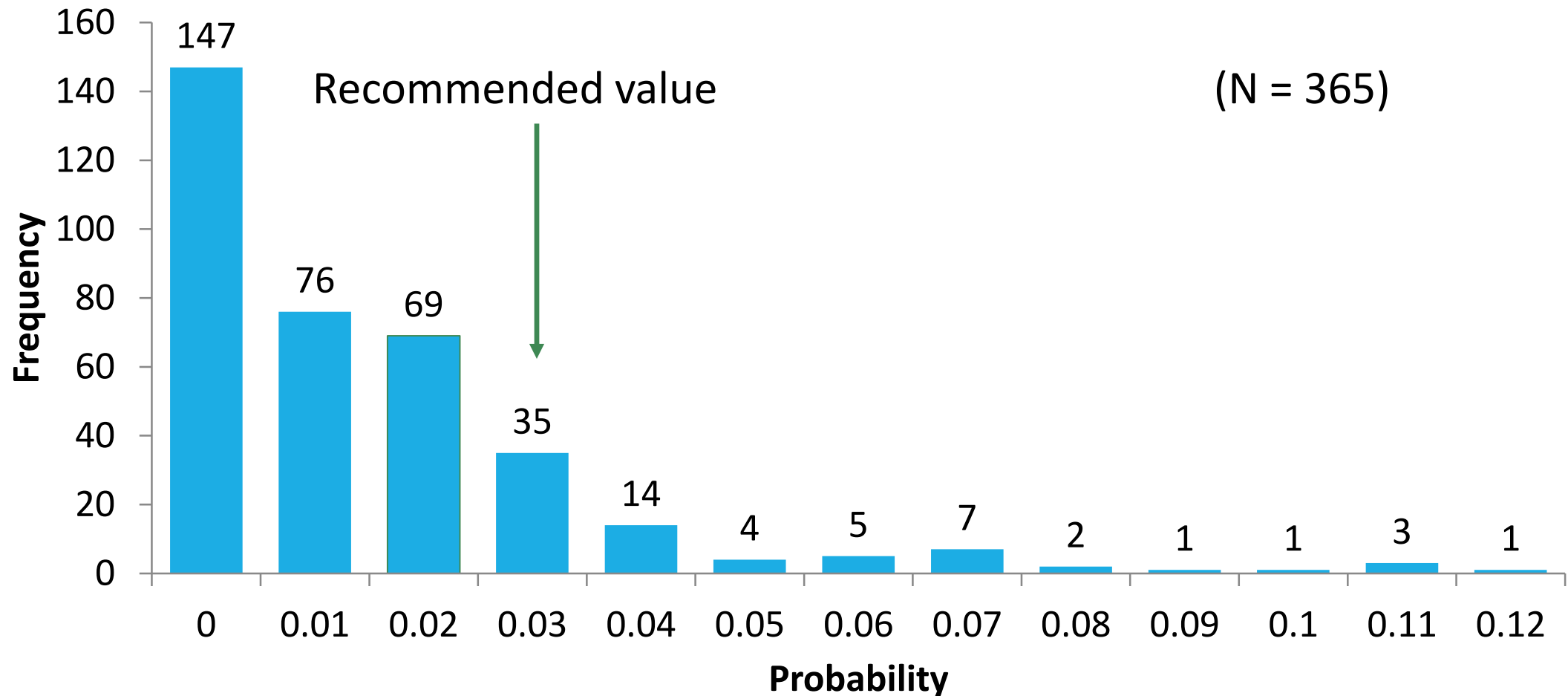


# Probability of Shower Use





# Distribution of Shower $p$ values for Homes with 2 residents



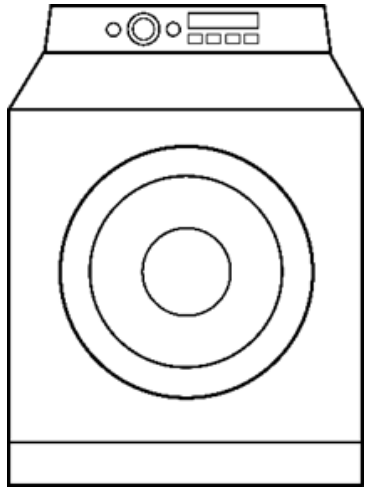
# Summary Probability of Fixture of Use

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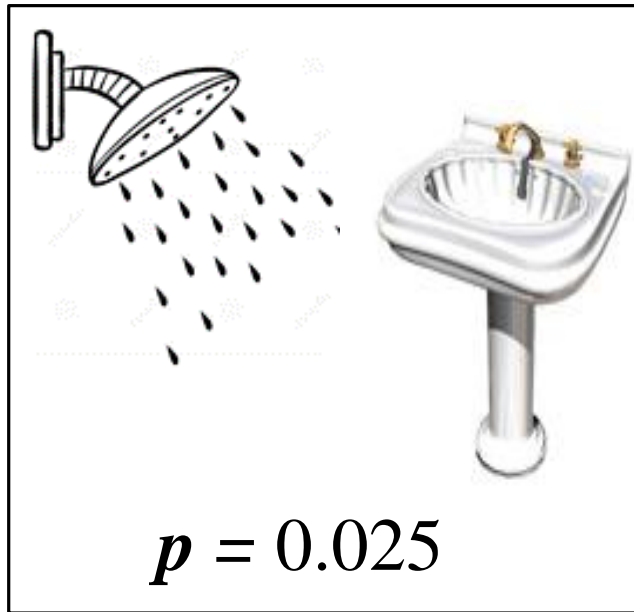
- ❖ Each fixture has a unique water use profile.
- ❖ Probability of fixture use does not dependent on how frequent a fixture used.
- ❖ Probability of fixture use increased as the number of residents increased.

# Design Fixture Probability Values

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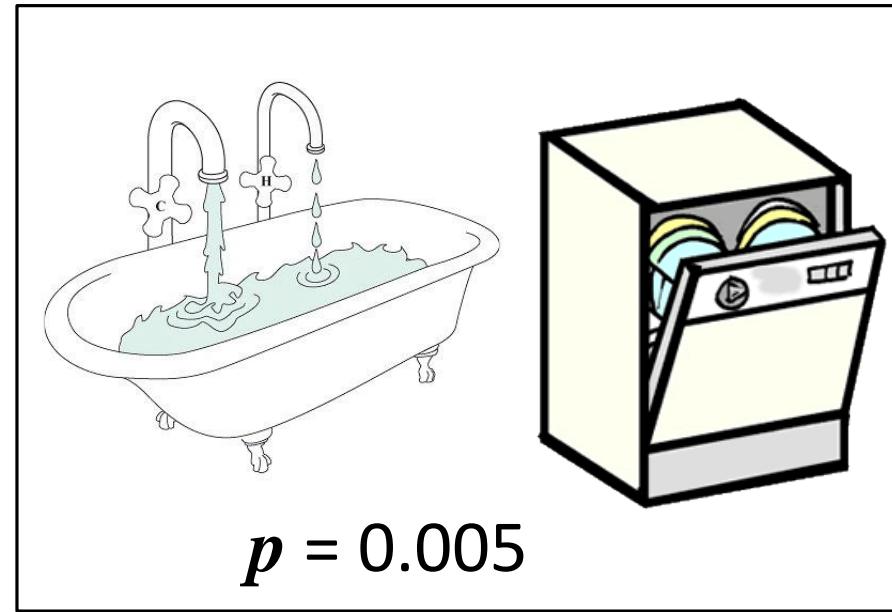
$p = 0.050$



$p = 0.025$



$p = 0.010$



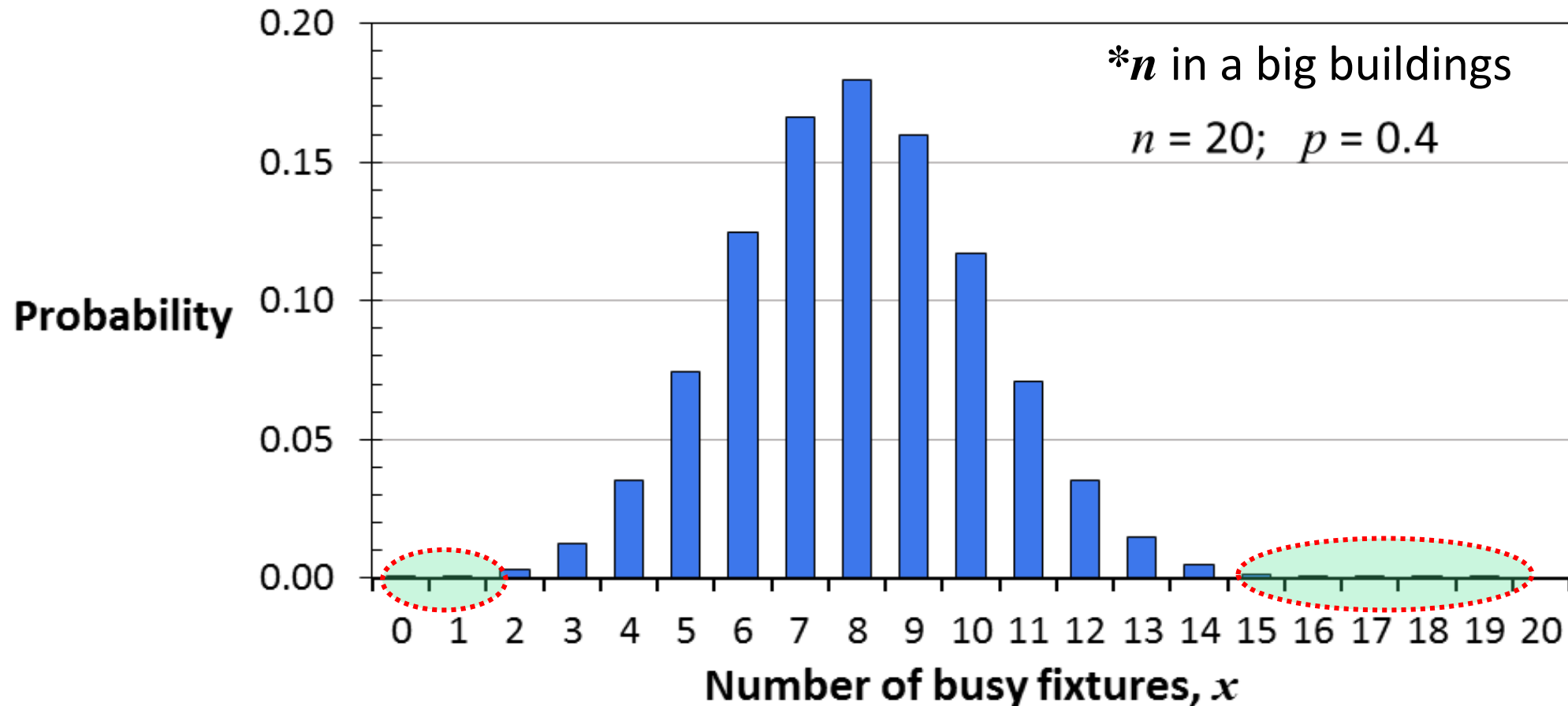
$p = 0.005$

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# APPLICATION

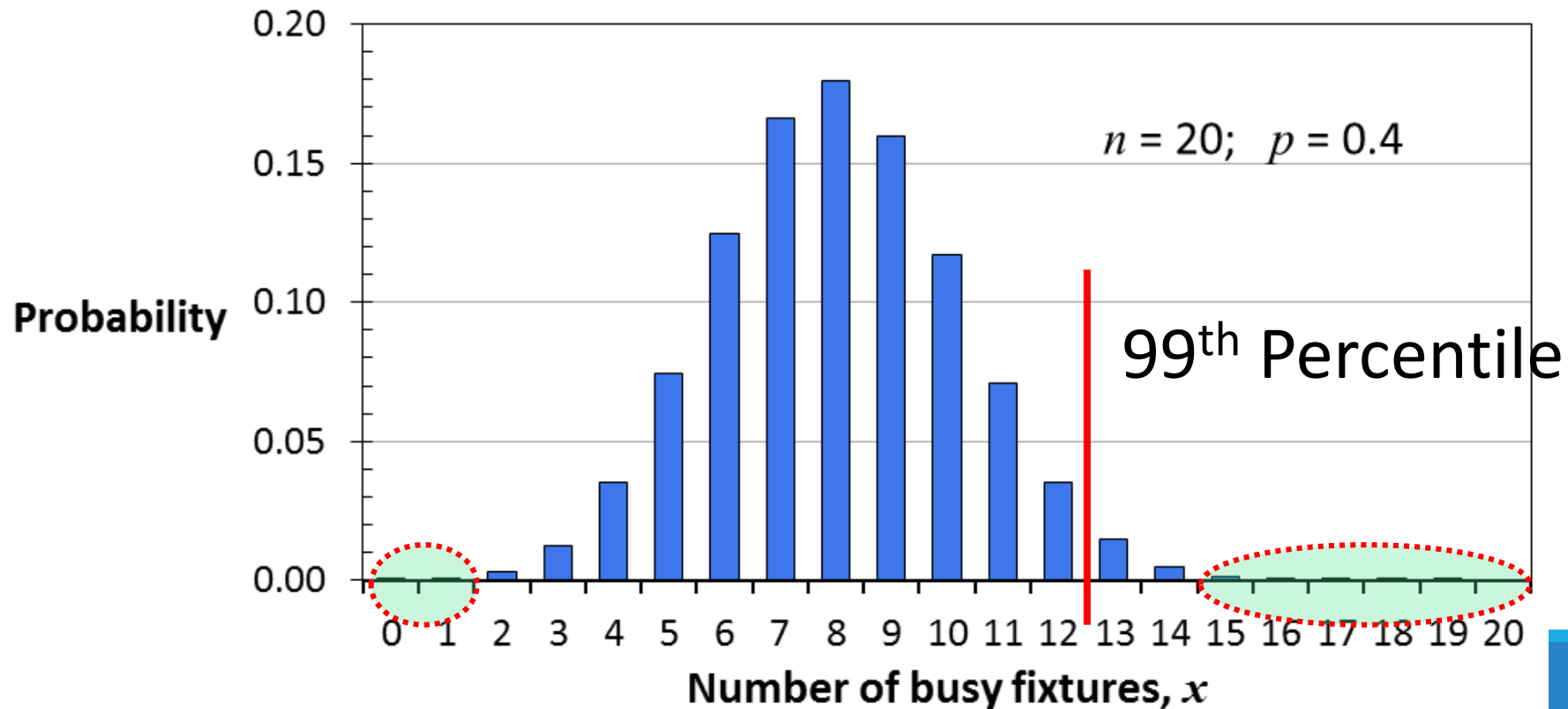
# Binomial Model

$$\Pr\left(\begin{array}{l} \text{exactly } x \text{ busy} \\ \text{out of } n \text{ fixtures} \end{array}\right) = \binom{n}{x} p^x (1-p)^{n-x}$$



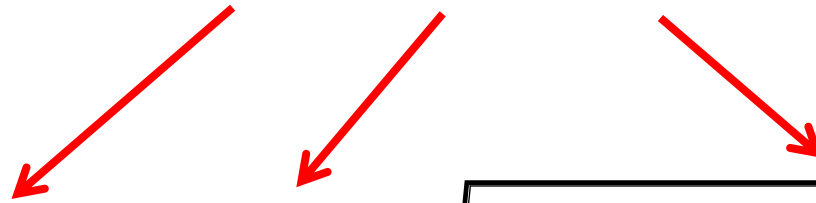
# “Frequency Factor” Approach

$$x = \text{Mean} + (z_{0.99}) \text{Standard Deviation}$$

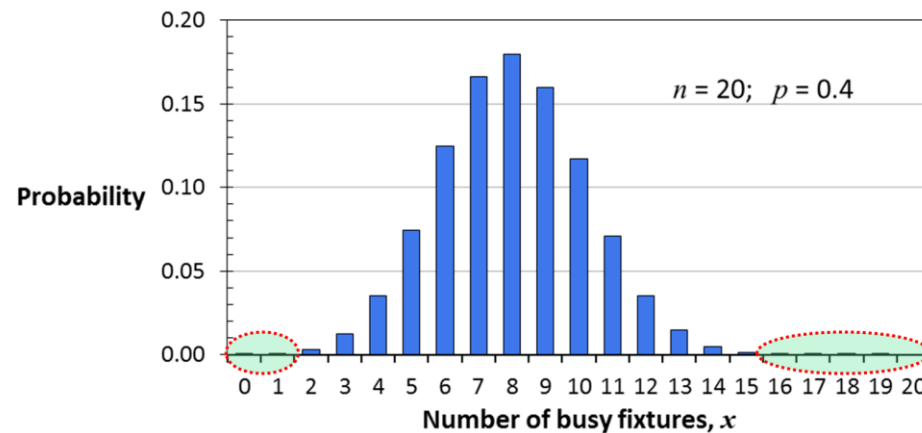


# Normal Approximation of Peak Flow

$$Q_{0.99} = \mu_q + (z_{0.99})\sigma_q$$

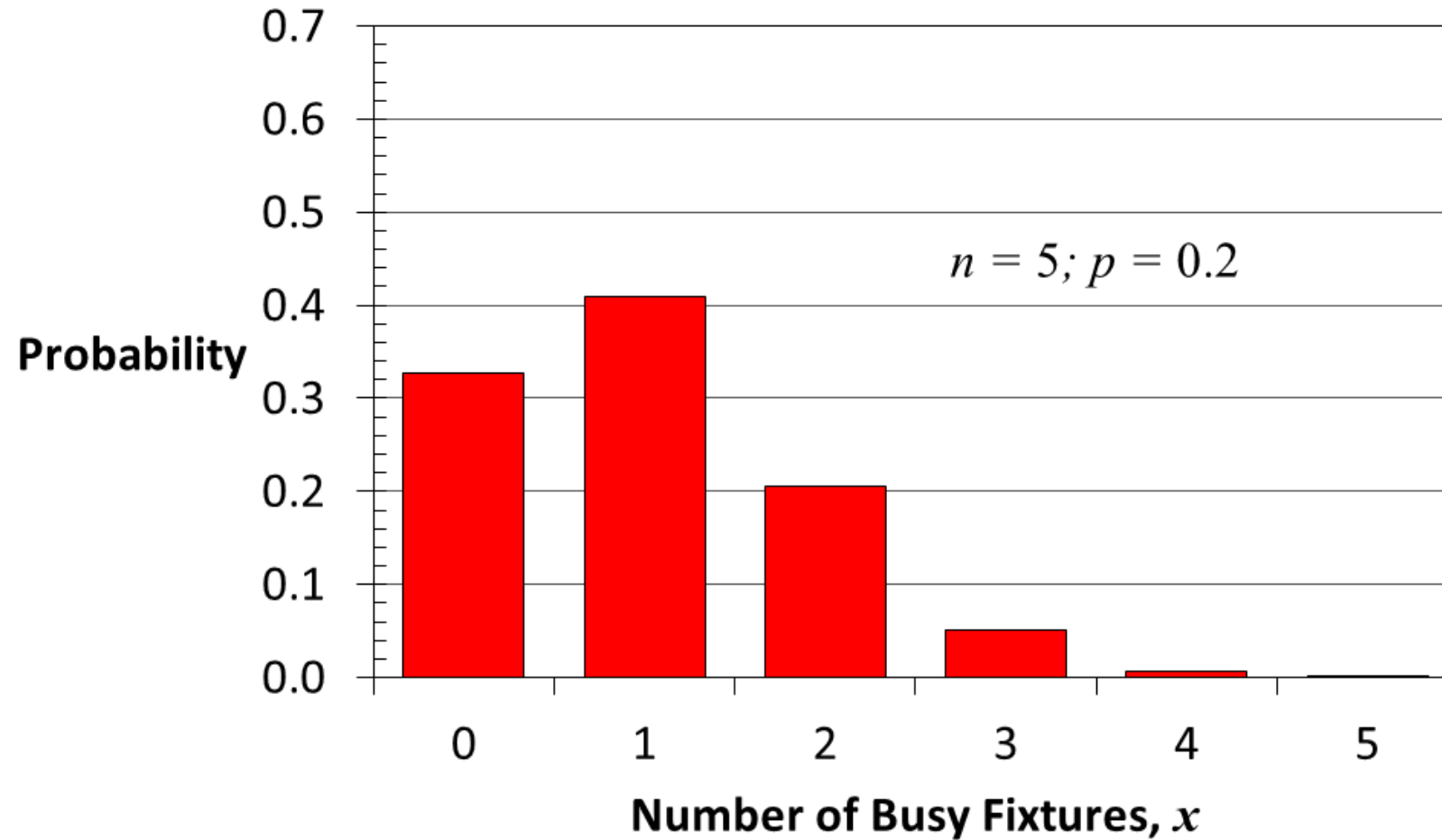


$$Q_{0.99} = \sum_{k=1}^K n_k p_k q_k + (z_{0.99}) \sqrt{\sum_{k=1}^K n_k p_k (1-p_k) q_k^2} \quad \text{- Wistort (1995)}$$



# Binomial Distribution

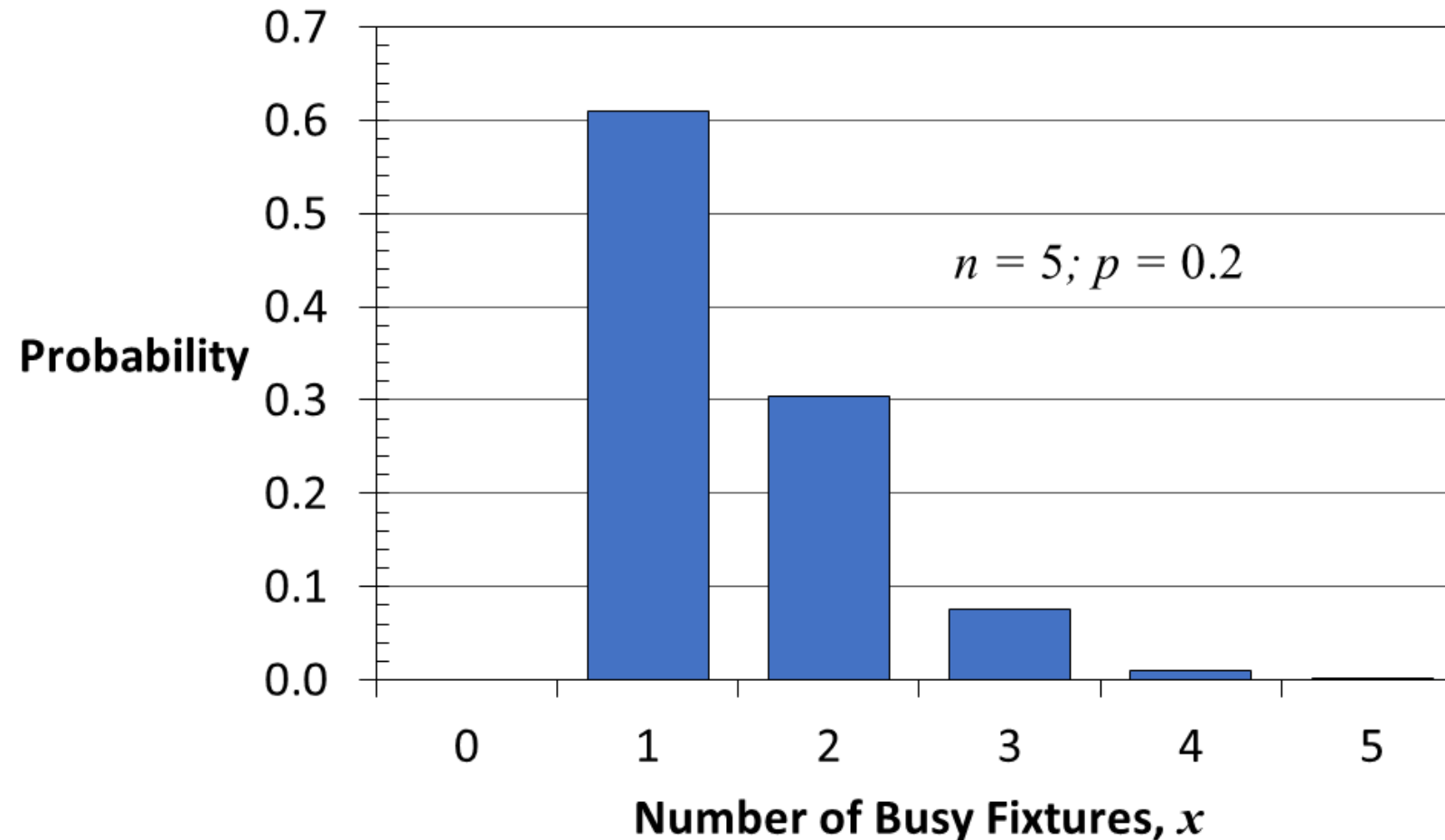
\* $n$  in a small buildings





# Zero Truncated Binomial Distribution (ZTBD)

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# Modified Wistort's Model

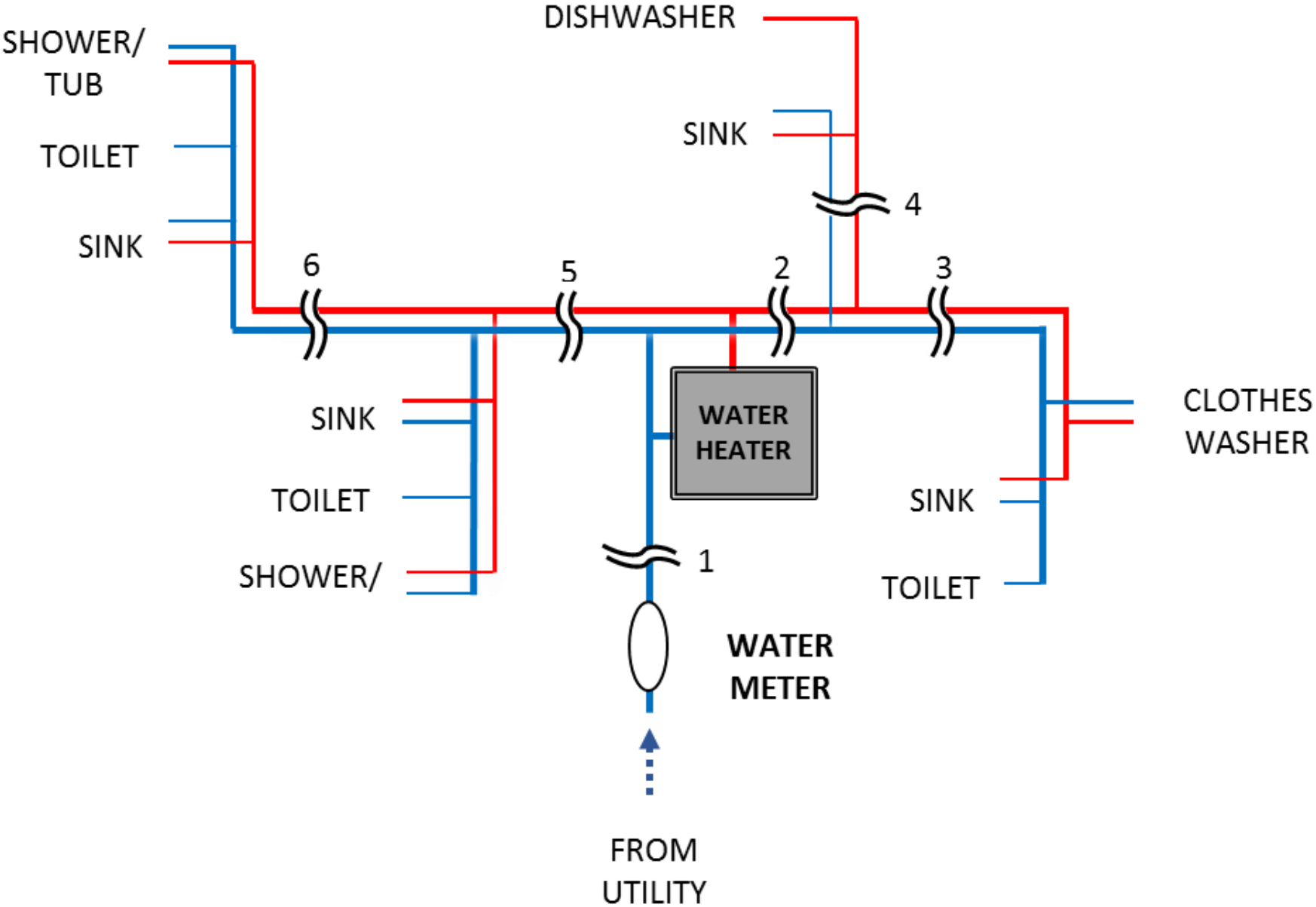
$$Q_{0.99} = \sum_{k=1}^K n_k p_k q_k + (z_{0.99}) \sqrt{\sum_{k=1}^K n_k p_k (1-p_k) q_k^2}$$

$$Q_{0.99} = \frac{1}{1-P_0} \left[ \sum_{k=1}^K n_k p_k q_k + (z_{0.99}) \sqrt{\left[ (1-P_0) \sum_{k=1}^K n_k p_k (1-p_k) q_k^2 \right] - P_0 \left( \sum_{k=1}^K n_k p_k q_k \right)^2} \right]$$

❖ Note:

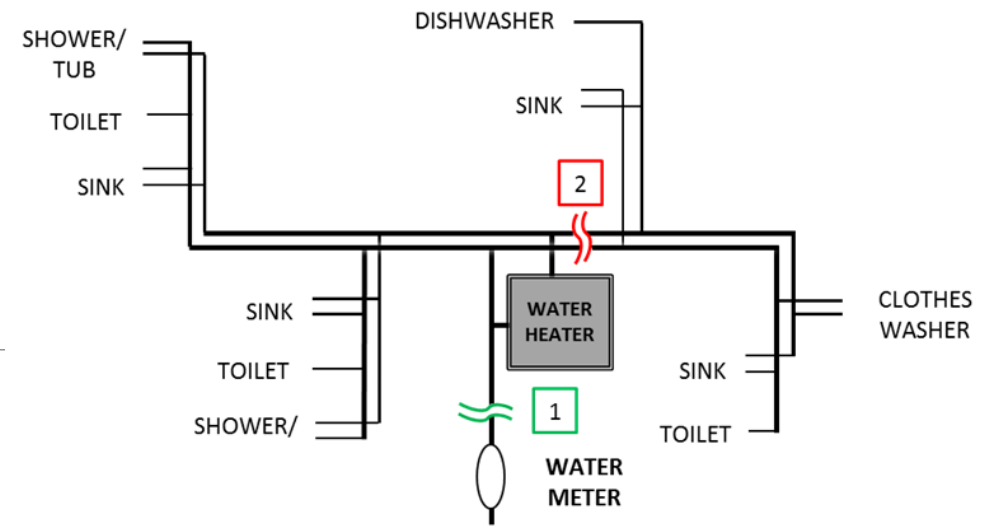
- ❖  $P_0 = \prod_1^k (1-p_k)^{n_k}$  is probability of stagnation in a home (i.e. no water use)
- ❖ Addresses water demand in single family homes with high  $P_0$
- ❖ Transitions back to Wistort's model as  $P_0$  approaches 0

# Hypothetical Residential Building Pipe Layout



# Peak Flow Calculations

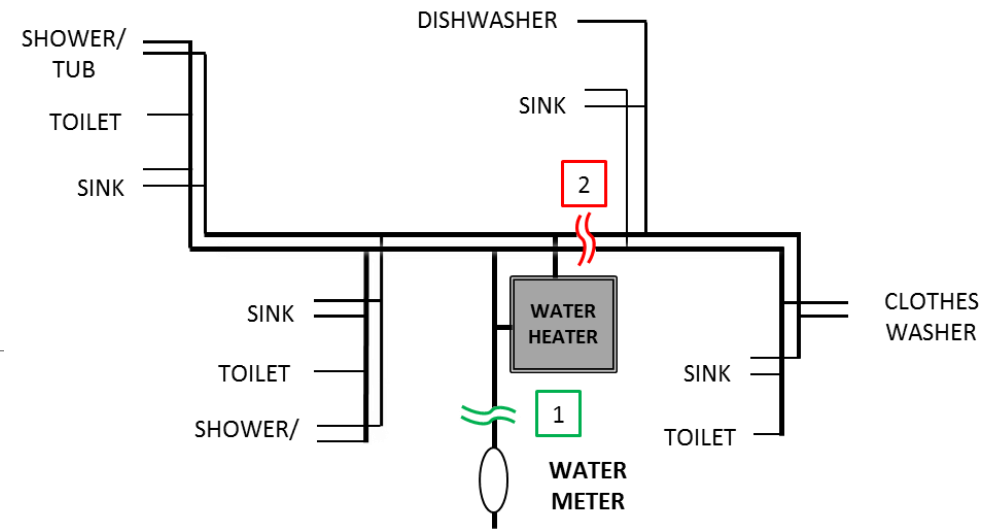
Example: 2.5 bath single family home



Section	UPC FU	UPC Method (gpm)	MW Method (gpm)
1	25.5	18.0	<b>11.8</b>
2	10.5	8.5	<b>6.9</b>

# Sizing Pipes

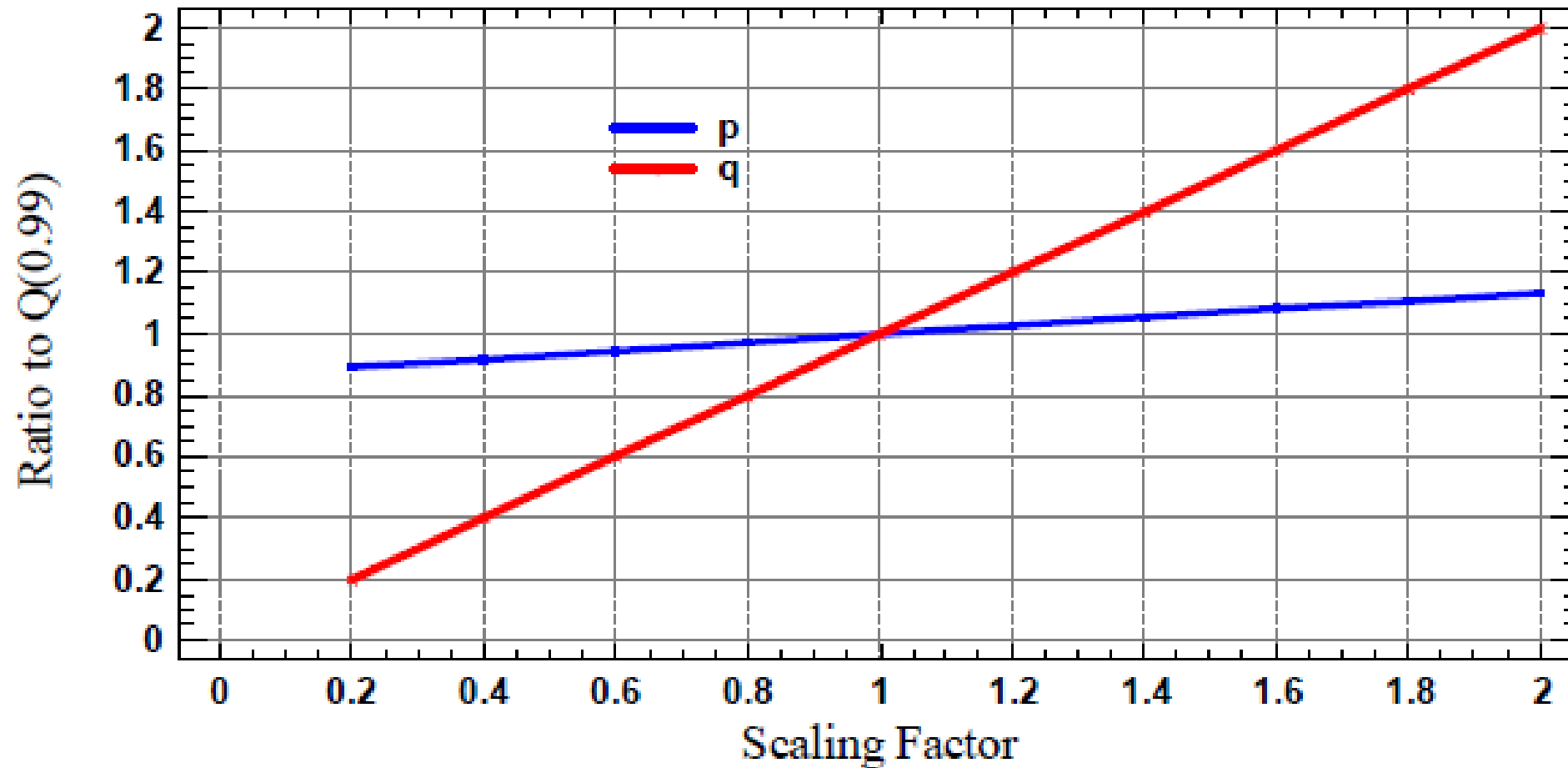
Example: 2.5 bath single family home



Section	UPC Method	Pipe Size*	MW Method	Pipe Size*
<b>1</b>	18.0 gpm	1"	11.8 gpm	3/4"
<b>2</b>	8.5 gpm	3/4"	6.9 gpm	3/4"

\* Maximum flow rate at 8 f/s

# Demand Sensitivity to $p$ and $q$ values



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# CONCLUSION

# Conclusion

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- ❖ Introduced a computational model to estimate peak water demand in single and multi-family dwellings.
- ❖ Recommended fixture  $p$  and  $q$  values.
- ❖ Model applicable to a wide spectrum of buildings.





# Questions?

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**University of Cincinnati**



